

TM-1063

Group Problem Solving by Autonomous  
Agents for Task Allocations Problem

by

S. Shindo & M. Sumida (Mitsubishi)

June, 1991

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Mita Kokusai Bldg. 21F  
4-28 Mita 1-Chome  
Minato-ku Tokyo 108 Japan

(03)3456-3191~5  
Telex ICOT J32964

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**Institute for New Generation Computer Technology**

# Group Problem Solving by Autonomous Agents for Task Allocation Problem

Seiichi SHINDO     Masato SUMIDA

Central Research Laboratory  
Mitsubishi Electric Corporation  
8 1-1, Tsukaguchi-Honmachi, Amagasaki, Hyogo, 661 JAPAN

## Abstract

We have developed a group problem solving method called ITM(Iterated Task Migration) for dynamic task allocation problems. ITM takes unoptimal task allocation to agents as input, then the agents try to change their task allocations toward the globally optimal allocation by iteration of task migrations. The cooperation by the agents offers the advantages of adaptability and parallelism, which contribute to solving the dynamic task allocation problems. ITM works in two ways, in a synchronized way(called ITM-S) and in an asynchronized way(called ITM-A). To evaluate ITM-S and ITM-A, we have applied them to the trouble recovery problem in the area of transportation. This paper describes the algorithms of ITM-S and ITM-A, and their evaluations by the experimental results.

## 1 Introduction

Task allocation problems, which decide allocation of tasks to resources to achieve constraint-satisfied or optimal/semi-optimal solution, are one of fundamental problems in many fields such as engineering. They are divided into two categories:

- *the static characteristic problem*: generation of a plan before the allocated tasks are executed.
- *the dynamic characteristic problem*: modification of the plan during the execution of the tasks because of changes of situation.

How to reduce the amount of computation by avoiding combinatorial explosion is important in solving them. For this requirement, two approaches have been researched, the one is based on mathematical programming[7] and the other is based on knowledge engineering[2][4]. In both of them, the dynamic problems in the above categories are less studied than the static problems. One of the major requirements for the dynamic problems is quick response. If in the time required to reach a solution the situation changes, then the solution can no longer be applied. Difficulty in solving the dynamic problems mainly comes from the treatment of time.

For the dynamic problems, we have taken group problem solving approach[1]. In this approach, a group of autonomous entities called agents(e.g., men or computers) act cooperatively, so that the group, as a whole, keeps its consistencies or achieves its goals.

The advantages of this approach are adaptability to environments and parallelism, which contribute to solving the dynamic problems.

Researches in the group problem solving have been done. However, they are concepts[6] or languages[3][5], therefore, they are too general to supply appropriate representation or effectiveness when they are applied to specific tasks or domains. In order to establish methods for a specific task, we have developed a group problem solving method especially for dynamic task allocation problems, called ITM(Iterated Task Migration).

This paper describes the framework of *ITM* and its evaluation by experimental results. The research was done as part of the Fifth Generation Computer Systems project of Japan.

## 2 Task Allocation Problems

In this section, we show the task allocation problem ITM treats. Some terms are defined below:

- a set of resources:  $RS = \{R_1, R_2, \dots, R_m\}$
- a set of tasks:  $TS = \{T_1, T_2, \dots, T_n\}$
- a subset of the tasks, allocated to  $R_i$ :  $TALC(R_i)$   
for  $\forall i, \forall j (i \neq j), TALC(R_i) \cap TALC(R_j) = \phi$
- $R_i$ 's function for evaluation:  $EVF_{R_i}(TALC(R_i))$

A resource uses its EVF to evaluate the allocated tasks.  $EVF_{R_i}$  maps  $TALC(R_i)$  onto non-negative value. EVFs may be either identical or different among the resources.

The problem is as follows:

Given  $RS$ ,  $TS$  and  $EVF(R_i)$  for  $\forall i$ , then find  $TALC(R_i)$  for  $\forall i$  which minimize  $\sum_{k=1}^m EVF_{R_k}(TALC(R_k))$  as possible. In addition, resources or tasks may be added or removed before the solution is found.

## 3 Overview of ITM

For the problem described in the previous section, ITM, based on mutual interaction among autonomous agents, tries to change initial task allocations towards better ones. ITM takes unoptimal task allocation to agents(corresponding to resources one to one) because of changes of resources or tasks, as input. Then the agents try to change their task allocations toward the globally optimal allocation by iteration of task migrations among them through the exchanges of messages. As the iteration proceeds, the result of the re-allocation is improved. A sketch of ITM's behavior is shown in figure 1.

The agents are assumed to be able to communicate each other. Each of them locally has the information on the current tasks allocated, its EVF and other agents' names. Other information can be acquired by the exchanges of the messages. The control

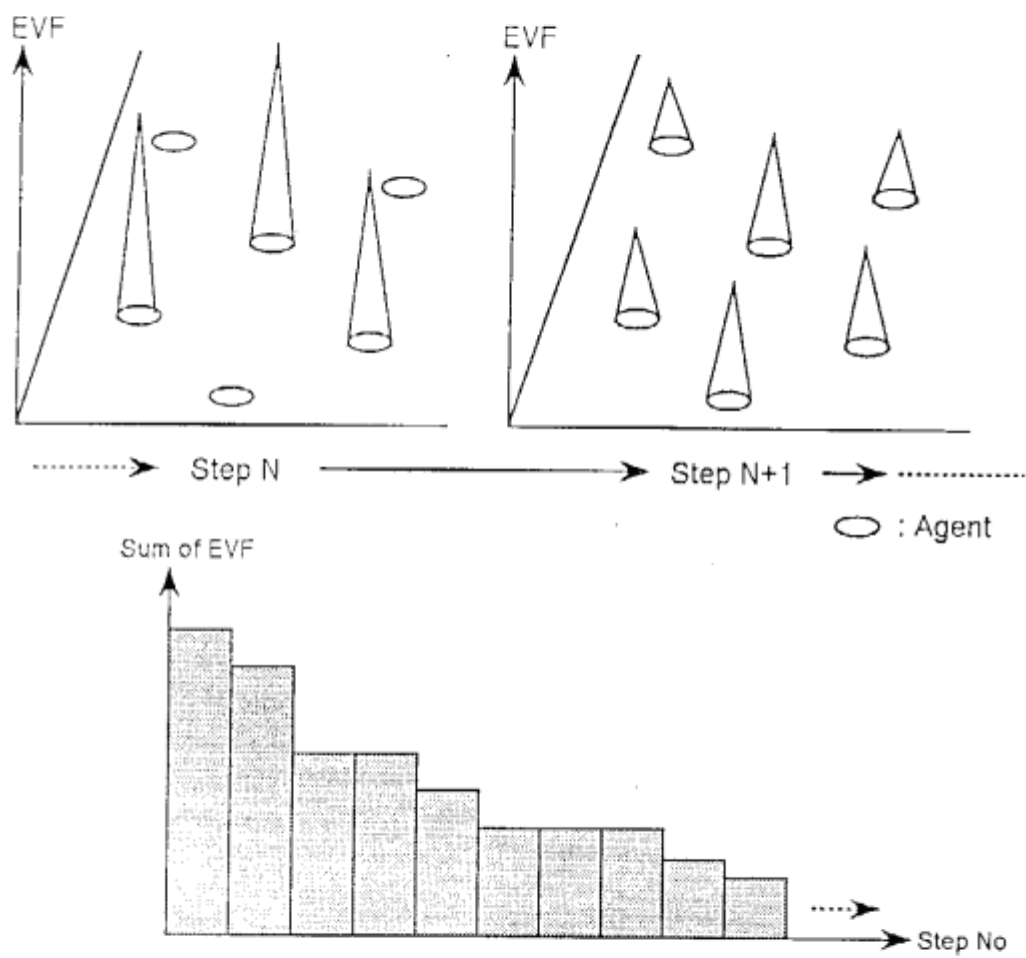


Figure 1: Sketch of Behavior of ITM

mechanism for these cooperative agents is an extension of contract net[3], i.e., a sequence of task announcement, bid and award. We call this sequence a task migration step.

Since ITM is based on a group of loosely-coupled autonomous agents, it offers the following advantages:

- *adaptability*: Agents are rather independent, and each of them has the cooperation mechanism, so that they continue to search for a better task allocation, in spite of changes of agents or tasks during the search.
- *parallelism*: Each agent may act in parallel, so that it needs less time to reach the new task allocation.
- *built-in search strategy*: In general, problem solving for these kinds of problems requires knowledge about controlling search, to avoid combinatorial explosion. However, there are problems which are too complex to extract the knowledge. ITM's built-in search strategy can be applied to such hard problems.

ITM works in two ways, in a synchronized way(called ITM-S) and in an asynchronized way(called ITM-A). In the next two sections, they are described in detail.

## 4 ITM-S

In ITM-S, the task migration step is iterated synchronously among agents. First, the task announcement phase occurs simultaneously in all agents, followed by the bid phase, then the agents change their task allocations. After that, the next task migration step begins simultaneously.

Here are shown the definitions of some terms used in the description of ITM.

- *overloaded* : An agent whose EVF value is positive is called an overloaded agent.
- $dEVF(A, SignT)$ : The amount of the decrease of an agent  $A$ 's EVF value because of migration of a task  $T$ . Negative value represents the increase of the EVF value. Sign is "+" or "-". "+" means that  $T$  is added to  $A$ . "-" means that  $T$  is removed from  $T$ .

The procedure for one task migration step of ITM-S is shown below:

1. *Task announcement*: An agent  $A_P$  checks if it is overloaded by computing  $EVF_{A_P}(TALC(A_P))$ .
  - *If  $A_P$  is overloaded*:  $A_P$  selects a task  $T_P$  from the current  $A_P$ 's tasks, such that  $dEVF(A_P, -T_P) > 0$  and  $dEVF(A_P, -T_P)$  is the largest. Then  $A_P$  broadcasts the task announcement message including the contents of  $T_P$  and  $dEVF(A_P, -T_P)$ , to call for candidates to execute  $T_P$  instead of  $A_P$ . If  $A_P$  cannot find such a task,  $A_P$  broadcasts the retirement message to show that  $A_P$  doesn't call for candidates in this task migration step,
  - *If  $A_P$  is not overloaded*:  $A_P$  broadcasts the retirement message.

2. *bid*: By receiving the task announcement messages or the retirement messages from all other agents, each of the agents can classify that the other agents into two classes, i.e., a manager(calling for candidates) and a contractor(not calling for candidates). An agent  $A_Q$  reacts to the task announcement message from  $A_P$  as follows:  $A_Q$  computes  $CON(A_P, A_Q)$  and replies to  $A_P$  with the bid message including  $CON(A_P, A_Q)$ .  $CON$  represents the amount of the change of sum of two agents' EVF values by migration of a task from the one to the other.  $CON(A_M, A_C)$  is equal to

$$dEVF(A_M, -T_M) + dEVF(A_C, +T_M)$$

where  $A_M$  is a manager,  $A_C$  is a contractor, and  $T_M$  is one of  $A_M$ 's tasks.

3. *bid sharing*: The managers receive the bid messages including  $CON$  values. Then, to assure globally conflict free and optimal task allocations in this task migration step, they share their  $CON$  values by sending the messages each other.
4. *award*: After sharing  $CON$  values about all agents, each of the managers independently tries to find an agent to which its announced task is allocated, under the condition of satisfying no-conflict and optimality. There may be some managers who cannot find such an agent because of this condition. After the selection, each of the managers broadcasts the award message to show which agent is selected, then the involved agents change their task allocations.

Sum of all agents' EVF values decreases by sum of  $CON$  values involved in the task migrations. The iteration of the task migration step terminates when each of the overloaded agents has no task to be announced.

Behaviors of the agents according to ITM-S is shown in figure 2.

- *In the task announcement phase*: An overloaded agent  $A_1$  selects a task  $T_1$  such that  $dEVF(A_1, [-T_1])$  is the largest, then sends the task announcement message to  $A_2$ ,  $A_3$  and  $A_4$ . A non-overloaded agent  $A_2$  sends the retirement message to  $A_1$ ,  $A_3$  and  $A_4$ .
- *In the bid phase*:  $A_2$  computes  $CON(A_1, A_2)(= dEVF(A_1, -T_1) + dEVF(A_2, +T_1))$ , then replies to  $A_1$  with the bid message including  $CON(A_1, A_2)$ .  $A_2$  also replies to  $A_3$  with the bid message including  $CON(A_3, A_2)$ .  $A_1$ , though it is overloaded, replies to  $A_3$  as well.
- *In the bid sharing phase*:  $A_1$  sends  $CON(A_1, A_2)$ ,  $CON(A_1, A_3)$  and  $CON(A_1, A_4)$  to  $A_3$ .  $A_3$  sends  $CON(A_3, A_1)$ ,  $CON(A_3, A_2)$  and  $CON(A_3, A_4)$  to  $A_1$ .
- *In the award phase*: By using the  $CON$  values,  $A_1$  finds  $A_2$  to allocate  $T_1$  and broadcasts the award message telling that  $T_1$  is re-allocated from  $A_1$  to  $A_2$ . Similarly  $A_3$  broadcasts the award message telling that  $T_3$  is re-allocated from  $A_3$  to  $A_4$ . these task re-allocations decrease  $CON(A_1, A_2) + CON(A_3, A_4)$  from sum of EVF values of all agents.

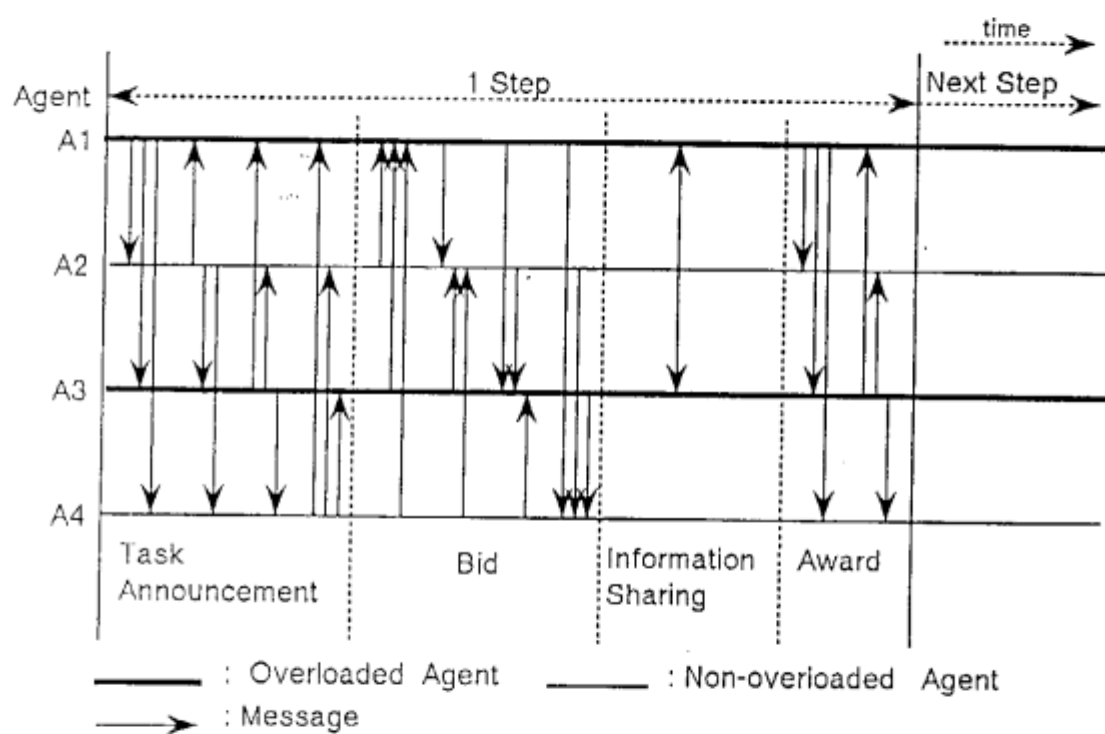


Figure 2: Behavior of ITM-S Agents

The advantage of ITM-S is adaptability. Since every task migration step begins simultaneously, therefore, at that time, ITM-S is open to increase or decrease of agents or tasks during the problem solving. For instance, An overloaded agent because of unexpectedly allocated tasks tries to decrease sum of EVF values of all agents by sending task announcement message.

## 5 ITM-A

In ITM-A, agents act asynchronously, e.g., some are in the task announcement phase, while others are in the bid phase. Similarly to ITM-S, the task migration step begins with checking if each of the agents checks if it is overloaded.

### (i) Procedure for non-overloaded agent

Consider a non-overloaded agent  $A_P$ .

1. *TA-waiting*:  $A_P$  waits for the task announcement message from other agents.
2. *bid*: When  $A_P$  receives the task announcement message from an agent an overloaded agent  $A_Q$ ,  $A_P$  evaluates the announced task by computing  $CON(A_Q, A_P)$ . If  $CON(A_Q, A_P) > 0$ ,  $A_P$  replies to  $A_Q$  with the bid message including  $CON(A_Q, A_P)$ , to register as the candidates for executing the announced task. Because, for  $A_P$  to execute the announced task instead of  $A_Q$  reduces the sum of EVF values of  $A_P$  and  $A_Q$ . After that,  $A_P$  waits for the award message in the A-waiting stage. If  $CON(A_Q, A_P) \leq 0$ ,  $A_P$  replies to  $A_Q$  with the rejection message, to show that  $A_P$  gives up registering as the candidates. After that,  $A_P$  waits for another task announcement message in the TA waiting phase again.
3. *A-waiting*:  $A_P$  waits for the award message from  $A_Q$ .
4. *award*:  $A_P$  receives the award message from  $A_Q$ . If the task is allocated to  $A_Q$ ,  $A_Q$  modifies its task allocation.

To prevent double bidding, Any task announcement messages reached in the A-waiting phase or the award phase, is replied with the rejection message.

### (ii) Procedure for overloaded agent

Consider a non-overloaded agent  $A_Q$ .

1. *task announcement*: Similarly to ITM-S,  $A_Q$  selects a task to be announced and broadcasts the task announcement message to call for the candidates. If  $A_Q$  finds no task to be announced, it sends no message.
2. *B-waiting*:  $A_Q$  waits for the replies(bid messages or the rejection messages) from the other agents.
3. *award*: After receiving all the replies,  $A_Q$  selects an agent  $A_R$  from the candidates, such that  $CON(A_Q, A_R)$  is the largest

Then  $A_Q$  sends the award message to all of the candidates to show that the announced task is allocated to  $A_R$ .



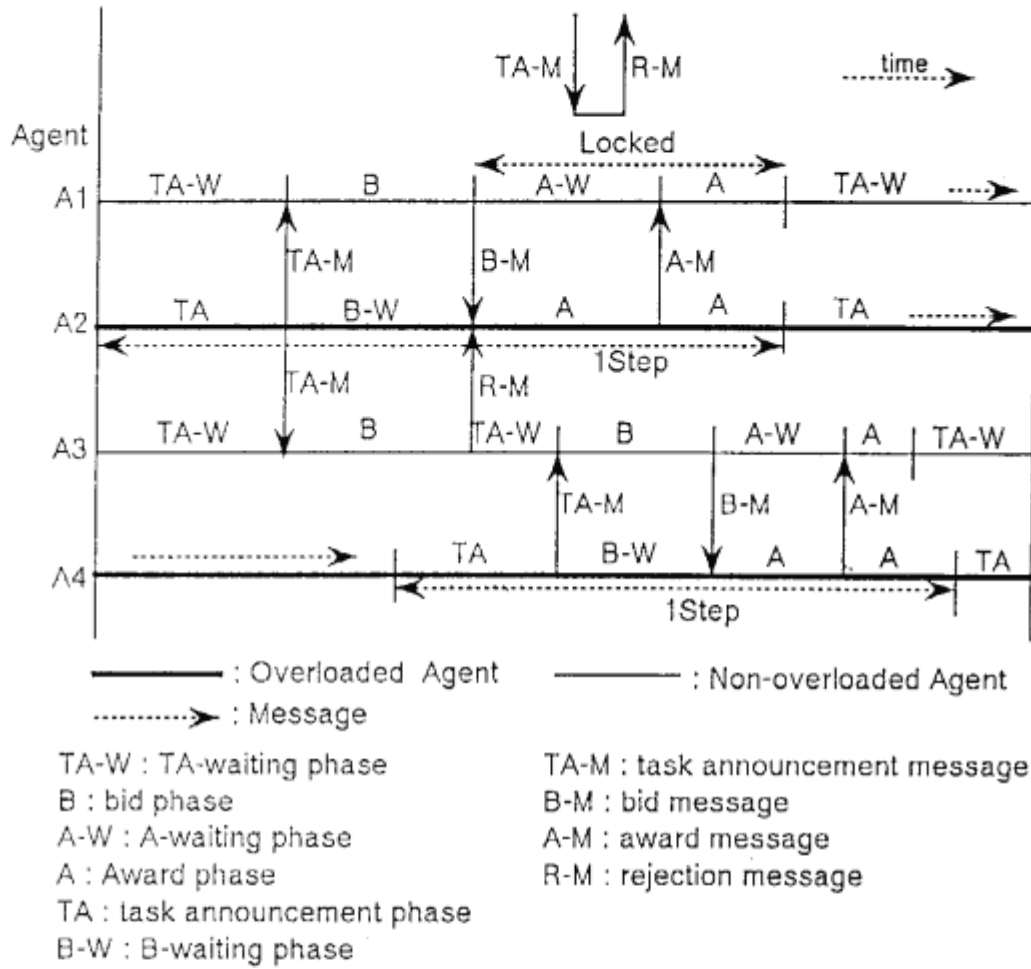


Figure 3: Behavior of ITM-A Agents

The iteration of the task migration step terminates when each of the overloaded agents has no task to be announced.

Behaviors of the agents according to ITM-A is shown in figure 3. An overloaded agent  $A_2$  broadcasts the task announcement message. Agents  $A_1$  and  $A_3$ , which are in the TA-waiting phase, evaluate the announced tasks. Since  $CON(A_2, A_1) > 0$ ,  $A_1$  replies to  $A_2$  with the bid message, then waits for the award message from  $A_2$ . Since  $CON(A_2, A_3) < 0$ ,  $A_3$  replies to  $A_2$  with the rejection message, then waits for another task announcement message.  $A_2$ , receiving the bid message only from  $A_1$ , sends the award message to  $A_1$ , then modifies its task allocation and goes to the next task migration step.  $A_1$ , receiving the award message from  $A_2$ , modifies its task allocation and waits for another task announcement message.  $A_3$  receives the task announcement message from  $A_4$ . This time, since  $CON(A_4, A_3) > 0$ ,  $A_3$  replies to  $A_4$  with the bid message, then, the interaction between  $A_3$  and  $A_4$  follows like that between  $A_1$  and  $A_2$ .

Comparing with ITM-S, ITM-A runs faster. This comes from less amount of time for synchronization and less amount of messages for information sharing. However, since ITM-A decides task allocations by less amount of information, ITM-A generally reduces sum of EVF values of all agents less than ITM-S.

## 6 Application

To evaluate ITM, we have applied ITM to the trouble recovery problem in the area of transportation. This section describes the problem domain.

Consider a group of trucks, each of which is delivering shipments with due-date requirements to many destinations. Initially, the shipments are appropriately allocated to the trucks so that they are delivered before their due-times. During the delivery, a trouble happens in one of the trucks, so that it can no longer carry its allocated shipments. The problem is to acquire new shipment allocations to the remaining trucks, in order to minimize the sum of over-due-times of all shipments because of the trouble.

The correspondence between ITM and the problem domain is shown below:

- *a task*  $\rightarrow$  a shipment.
- *an agent*  $\rightarrow$  a truck.
- *EVF*  $\rightarrow$  sum of the over-due-times of the shipments allocated to the truck. This value depends on the routing, i.e., the order of visiting the destinations. Each truck re-schedules its routing to minimize its total over-due-time.

In ITM, first, the shipments allocated to the truck in the trouble, are distributed randomly, then the task migrations follow towards minimizing sum of the over-due-times of the all shipments.

## 7 Experimental Results

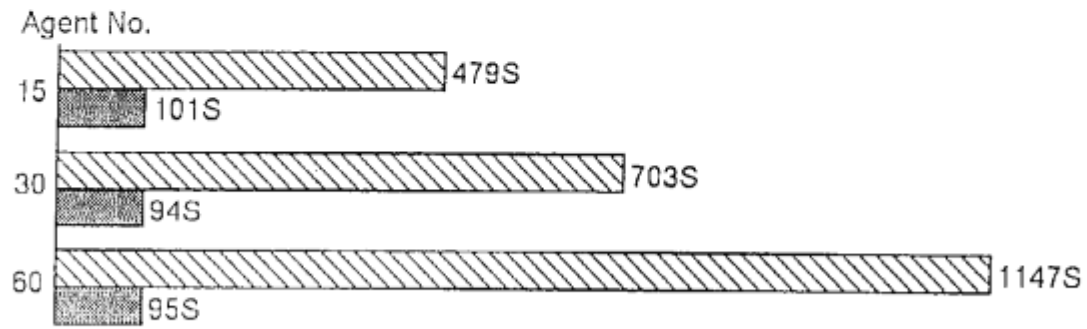
We have implemented ITM on the parallel inference machine MultiPSI[8], developed by ICOT. MultiPSI executes programs written in the parallel logic programming language KL1[8] in parallel, by a group of processor elements(called PEs) with no shared memory. We use 16PEs for our experiments with 15,30,60 trucks and about 1,200 shipments. The trucks' actions according to ITM are distributed onto PEs equally.

Figure 4 shows the total execution times and the final solution(sum of delay time).

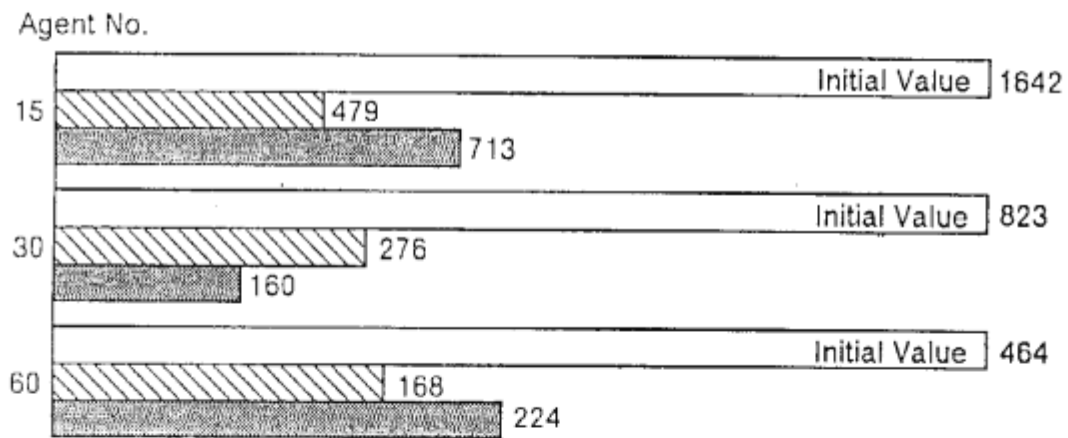
The total execution time by ITM-S is from 5 to 11 times much as that by ITM-A. ITM-S gives better final solution than ITM-A in the experiments with 15 and 60 trucks, and ITM-A gives better solution in the experiment with 30 trucks.

One of the criteria for quick response in dynamic problems is high speed and, if possible, good solution. From this viewpoint, ITM-A is more suitable than ITM-S, because of its extremely high speed comparing with ITM-S.

Another criterion is interactivensess, i.e., how easily or quickly the changes of the problem can be reflected in the course of the problem solving. ITM-S can reflect such changes at every point of the beginnings of the task announcement phases. ITM-A



(A) Total Execution Times (in Seconds)



(B) Final Solutions(normalized by initial values)

▨ : ITM-S    ▤ : ITM-A

Figure 4: Experimental Results

cannot reflect such changes, until the final solution without reflecting the changes, is acquired. Table 1 compares the response times of ITM-S and ITM-A, i.e., compares the average times for 1 task migration step by ITM-S with the total execution times by ITM-A. This table shows that, in all the cases, the response times by ITM-S is smaller than those by ITM-A. From the viewpoint of interactiveness, ITM-S is more suitable than ITM-A, because of its quicker response comparing with ITM-A.

agent no.	ITM-S	ITM-A
15	18s	101s
30	37s	94s
60	71s	95s

Table 1 Response times(in seconds) by ITM-S and ITM-A

## 8 Conclusion

This paper has described group problem solving methods ITM-A and ITM-S, for dynamic task allocation problems. Quick response is critical for the dynamic problems. Our experimental results have shown that ITM-S improves the adaptability of the group of the agents, while ITM-A improves the execution time of the group. The two factors contribute to improving the quick response.

ITM, based on a group of autonomous agents, can be well applied to distributed environments such as production scheduling among distributed factories and task distribution in computer networks.

On the other hands, ITM doesn't assure the optimality of its solutions. Therefore, ITM cannot be applied to the problems requiring strict optimality of the solutions. Another limitation is the number of agents. The more the number of the agents is, the more the amount of communication grows, which cause the drop of the response time. Clarifying the degree of the quality of the solution, and the relationship between the number of agents and the response times, remains to be done in the future.

## Acknowledgment

This research was done as one of the subprojects of the Fifth Generation Computer Systems(FGCS) project. We would like to thank Dr.K.Fuchi(Director of ICOT) for the opportunity of doing this research and Dr.K.Nitta(Chief of 7th Laboratory) and Dr.N.Ichiyoshi(Deputy Chief of 7th Laboratory for their advice and encouragement.

## References

- [1] Bond,A.H. and Gasser,L. *"Readings in Distributed Artificial Intelligence"* Morgan Kaufmann Publishers,Inc., California, 1988.
- [2] Cammarata,S., McArthur,D. and Steeb,R *"Strategies of Cooperation in Distributed Problem Solving"* Proc. of the 8th International Joint Conference on Artificial Intelligence, 1983, pp.767-770.

- [3] Davis,R. and Smith,R.G. *"Negotiation as a Metaphor for Distributed Problem Solving"* Artificial Intelligence Vol.20, 1983, pp.63-109.
- [4] Fox,M.S. and Smith,S.F. *"ISIS - a knowledge-based system for factory scheduling"* Expert Systems Vol.1, No.1, 1984, pp.25-49.
- [5] Gasser,L., Braganza,C and Herman,N. *"MADE: A flexible Testbed for Distributed AI Research"* Distributed Artificial Intelligence, Pitman Publishing/Morgan Kaufmann Publishers,Inc., London/California, 1987, pp.271-287.
- [6] Hewitt,C. *"Offices are open systems"* ACM Transactions on Office Information Systems, Vol.4, No.3, July 1986, pp.271-287.
- [7] Ibaraki,T. and Katoh,N. *"Resource Allocation Problems: Algorithmic Approaches"* The MIT Press, Cambridge, Mass., 1988
- [8] Nakajima,K., Inamura,Y., Ichiyoshi,N., Rokusawa,K. and Chikayama,T *"Distributed Implementation of KL1 on the Multi-PSI/V2"* Proc. of the 6th International Conference on Logic Programming, 1989, pp.436-451.