

TM-0892

Analogy by Simulation — a Weak  
Justification Method

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July, 1990

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# Analogy by Simulation - a Weak Justification Method

(PRELIMINARY REPORT)

EXTENDED ABSTRACT

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## Abstract

This paper is a preliminary report on a novel method for analogical reasoning. Davies points out a problem, called *the justification problem*, claiming that we should find a criterion which justifies the conclusion obtained by analogy. This paper takes a certain type of analogy, and discuss an answer of the problem. The central idea of this method is inspired by *simulation* and will be expressed as follows: *If a phenomenon observed in the unknown domain can be explained in the well-known domain, only the same mechanism which directly relates the explanation is assumed to work in the unknown domain.*

## 1 Introduction

When we explain a process of reasoning by analogy, we may say that "An object  $T$  is similar to another object  $S$  in that  $T$  shares a property  $P$  with  $S$ .  $S$  satisfies another property  $Q$ . Therefore,  $T$  satisfies  $Q$ , too", or it may be expressed more formally by a schema "If  $P(T) \wedge P(S) \wedge Q(S)$  holds, then  $Q(T)$  holds". Here,  $T$  will be called the *target*,  $S$  be the *source*,  $P$  be the *similarity* or *shared property* between  $T$  and  $S$ , and  $Q$  be the *projected property*.

Nevertheless, the above description of the process of analogy is insufficient. Researchers studying analogy have come to recognize the necessity to reveal some implicit knowledge which influences the process but does not appear in the above schema. T.R.Davies *et al.* [6] gives an intuitive example which shows the existence of such implicit knowledge: Bob's car and Sue's car are both the same type, but we could not infer that Bob's car is painted red just because Sue's car is painted red. From the fact that Sue's car is worth about \$3500, however, we may infer that Bob's car is worth about \$3500. It clearly suggests that the plausibility of the conclusion depends on some implicit knowledge that is not provided in the premiss and that is on the relation between the similarity and the projected property. To reveal such implicit knowledge which justifies some analogical inference is very important, because it prevents an syntactical application of an analogical schema from yielding useless conclusions.

This paper takes a certain type of analogical inference and proposes a novel method based on a logical criterion which weakly justifies the conclusion obtained by the analogy. The central idea is inspired by *simulation* and will be expressed as follows: *If a phenomenon observed in the unknown domain can be explained in the well-known domain, only the same mechanism which directly relates the explanation is assumed to work in the unknown domain.*

## 2 What is projected and how?

Justification of projecting a certain property has recently aroused the interest of researchers studying analogy [5, 6]. According to their approach, once we give the implicit knowledge for justification, analogy is collapsed just into deduction. This will be against our intuition (“analogy” is not deductive!). Here, we seek a weaker criterion for the justification which leaves analogy non-deductive.

### 2.1 The importance of precondition of causality in analogy

Importance of causality in analogy has been emphasized repeatedly [1, 2], for instance, Winston proposed a theory for analogy, where the causal structure of the source situation is assumed to map onto the target situation. When we consider causality more precisely, we may have a different standpoint, that is, any causalities govern every situations, however, whether the causalities may work actually depend on the hold of their precondition which are necessary when causalities influence some situations. Such view of causality has been taken in recent studies on reasoning about action [3, 4]. If we see analogy from this standpoint, we will notice that it is the precondition of causality rather than the causality itself that is mapped by an analogical process. One of the difficulties of clarifying such analogy is that the precondition is often implicit, that is, it may not appear explicitly in the description of the similarity.

### 2.2 Extracting implicit precondition from simulation

When we observe a situation, we often reason why the situation occurs by making use of some rules about the domain, causalities and, sometimes, knowledge about another well-known domain. For instance, when we need to infer something about another person, by putting ourselves in a certain situation which he occupies, we sometimes find a explanation of how and why he is what he is, and can conjecture unknown properties which he would satisfy, his present state, character, movements of his mind, the purpose of his action and his next action.

This type of inference is very common in human reasoning, sympathy will belong to this type, experiments by simulation may be considered as this case in the technological field and the inference has been seen in many papers on causal reasoning in the cognitive science fields [8, 9].

Such inference can be considered as a certain type of analogy, where the source is just each of ourselves, the target is he, the similarity is the fact that we have the possibility to cause a same phenomenon (otherwise, we could not explain why he do so), and projected properties are, essentially, preconditions which are needed in the explanation of the phenomenon, for instance, a precondition that he has the same type of mind as we have and that it governs all the process in the conjecture. What we conjecture above is deduced from the projected preconditions and known facts. Thus, we will easily extract possibly related implicit preconditions on the observed phenomenon from simulation in the well-known domain.

### 3 A Simulation Method

Using the following example, this section introduces a method for analogy by simulation.

#### Example

Hector feels pain when he is injured or burnt. Also, Brutus feels pain when he is injured. This may be represented as follows:

$$Has(Hector, Injury) \supset Feels(Hector, Pain)$$

$$\wedge Has(Hector, Burn) \supset Feels(Hector, Pain)$$

$$\wedge Has(Brutus, Injury) \supset Feels(Brutus, Pain)$$

In this case, we would conclude that Brutus feels pain when he is burnt by analogy, however, we would not conclude that Brutus is powerful even if Hector is powerful.

In this method, it is assumed that domain knowledge and knowledge about the source are given. Let knowledge be a set of first order sentences. It is divided into two subsets, a set  $D$  of sentences free from a particular object  $S$  and a set  $F(S)$  sentences in which  $S$  occurs.

In this paper, a *explanation* means a minimal deduction path from a particular premise to a particular conclusion, that is, if we remove a sentence from the premise, we can not find another deduction path in making use of the remainder premise.

The following is a detail of this method. It can be divided into four steps.

#### (1) Understanding Step:

From the domain knowledge  $d \in D$  and the source knowledge  $f_1(S) \in F(S)$ , a explanation how the source satisfies the shared property is made ( $f_1(S), d \vdash P(S)$ ), where  $f_1(S)$  and  $d$  are minimal set used in the explanation.  $f_1(S)$  will be called the *implicit premise* w.r.t.  $P$ , and  $d$  be the *implicit causal knowledge*.

$$d : \quad \forall x, i. (Animal(x) \wedge Has(x, i) \wedge Destructive(x, i) \supset Feel(x, Pain))$$

$$f_1(S) : \quad Animal(Hector) \wedge Destructive(Hector, Injury)$$

$$P(S) : \text{Has}(\text{Hector}, \text{Injury}) \supset \text{Feels}(\text{Hector}, \text{Pain})$$

(2) Mapping Step:

The implicit premise  $f_1(S)$  used in the above explanation is mapped into the target (that is, it is assumed that  $f_1(T)$  holds) if it does not cause inconsistency with knowledge about the target. That is, if it mapped, the target can be explained to satisfy the shared property by the same way in Understanding Step ( $f_1(T), d \vdash P(T)$ ) and its intuitive meaning is that the target has the same mechanism which works when how the source satisfies the shared property is explained.

$$f_1(T) : \text{Animal}(\text{Brutus}) \wedge \text{Destructive}(\text{Brutus}, \text{Injury})$$

(3) Justifying Relevance Step:

From the implicit causal knowledge  $d$  and the source knowledge  $f_1(S)$ , and additionally  $f_2(S) \in F(S)$ , this step tries to *infer* (not necessarily to *explain*) how the source satisfies the projected property  $Q$  ( $f_1(S), f_2(S), d \vdash Q(S)$ ). If possible,  $Q$  will be called *relevant* to  $P$  w.r.t.  $d$ . Also,  $f_2(S)$  will be called the implicit premise w.r.t.  $Q$ .

$$\begin{aligned} f_2(S) &: \text{Destructive}(\text{Hector}, \text{Burnt}) \\ Q(S) &: \text{Has}(\text{Hector}, \text{Burnt}) \supset \text{Feels}(\text{Hector}, \text{Pain}) \end{aligned}$$

(4) Projecting Step:

The implicit premise  $f_1(S)$  and  $f_2(S)$  are mapped into the target if it does not cause inconsistency with the target knowledge. If it mapped, the target can be explained to satisfy the projected property by the same way in Justifying Relevance Step ( $f_1(T), f_2(T), d \vdash Q(T)$ ), that is, it is conjectured that the target may have a property  $Q$ .

$$\begin{aligned} f_2(T) &: \text{Destructive}(\text{Brutus}, \text{Burnt}) \\ Q(T) &: \text{Has}(\text{Brutus}, \text{Burnt}) \supset \text{Feels}(\text{Brutus}, \text{Pain}) \end{aligned}$$

Here, note that other possible projected properties are

$$\text{Animal}(\text{Brutus}), \text{Destructive}(\text{Brutus}, \text{Injury}), \text{Destructive}(\text{Brutus}, \text{Burnt}), \dots$$

however, a property which does not relate the explanation in the source domain, like  $\text{Powerful}(\text{Hector})$  or  $\text{TwoEyes}(\text{Hector})$ , is prohibited from being projected, even assuming that  $\text{Powerful}(\text{Hector}) \in F(S)$  or  $\forall x. (\text{Animal}(x) \supset \text{TwoEyes}(x)) \in D$ .

## 4 Conclusion and Remarks

This paper proposes a novel logical method for analogical reasoning.

This method gives an answer to *the non-dedundancy problem* pointed out by Davies *et*

al. [6], the source instance should provide new information about the conclusion. If a conclusion obtained by this method is not deductive (for instance,  $Has(Brutus, Burnt) \supset Feels(Brutus, Pain)$ ,  $Animal(Brutus)$ ,  $Destructive(Brutus, Injury)$ , ... in the above example), it is a projected property shared by the source (*Hector*), which is represented in the source knowledge ( $F(S)$ ) or obtained from the domain knowledge additionally to the source knowledge. That is, the source information is actually used.

This method is general in that it is a logical approach independent from any particular system. In fact, it seems not to cause inconsistency to studies which have been reported, but to make their conclusions more selected. However, this method will not yield a certain type of analogy like the example of cars reported in the introduction, which is called *functional analogy* [7].

## References

- [1] Winston, P.H.: Learning Principles from Precedents and exercises, *Artificial Intelligence*, Vol. 19, No. 3 (1982).
- [2] Gentner, D.: Structure-mapping: Theoretical Framework for Analogy, *Cognitive Science*, Vol. 7, No. 2 (1983) 155-170.
- [3] Lifschitz, V.: Formal Theories of Action, in *Proc. of The Frame Problem Workshop 87* (1987) 35-57.
- [4] Georgeff, M.P.: Many Agents Are Better than One, in *Proc. of The Frame Problem Workshop 87* (1987) 59-75.
- [5] Keder-Cabelli, S.: Purpose-directed analogy, in *the 7th Annual Conference of the Cognitive Science Society*, Hillsdale, NJ: Lawrence Erlbaum Associates (1985) 150-159.
- [6] Davies, T. & Russel, S.J.: A logical approach to reasoning by analogy, in *IJCAI-87* (1987) 264-270.
- [7] Collins, A., Warnock, E.H., Aiello, N., & Miller, M.L.: Reasoning from incomplete knowledge, In D.G. Bobrow and A. Collins (Eds.), *Representation and understanding: studies in cognitive science*, New York: Academic Press (1975).
- [8] Kanouse, D.E.: Language, labeling, and attribution, In E.E. Jones, D.E. Kanouse, H.H. Kelley, R.E. Nisbett, S. Valins & B. Weiner (Eds.), *Attribution: Perceiving the causes of behavior*, General Learning Press (1972) 121-135.
- [9] Nisbett, R.E. & Ross, L.: *Human inference: Strategies and shortcomings of social judgement*, Prentice-Hall (1980).